

## An Introduction to Spatial Data Analysis

Luc Anselin, PhD
Julia Koschinsky
University of Illinois, Urbana-Champaign

Spatial Analysis Laboratory http://sal.uiuc.edu

#### The GeoDa Team

- Luc Anselin: Overall Direction
- Ibnu Syabri: EDA and ESDA, Flows
- Youngihn Kho: 3D Visualization, Graphics
- Yun-Tien Lee: Cross-Platform, wxWidgets
- Julia Koschinsky: Documentation and Training

## Acknowledgments

- National Science Foundation
  - © Center for Spatially Integrated Social Science
- National Cancer Institute
- Association of Teachers of Preventive Medicine / Centers for Disease Control

#### Outline

- Why Background
- How Functionality
- What is Next

## Background

Copyright © 2005 by Luc Anselin, All Rights Reserved

#### CSISS

- © Center for Spatially Integrated Social Science
  - NSF Infrastructure Project 1999-2004
  - headquartered UC Santa Barbara
  - Software Tools Program at UIUC
- Mission
  - promote spatial thinking and spatial analysis in social science

http://www.csiss.org/

## Center for Spatially Integrated Social Science Spatial Resources for the Social Sciences

The CSISS Mission recognizes the growing significance of space, spatiality, location, and place in social science research. It seeks to develop unrestricted access to tools and perspectives that will advance the spatial analytic capabilities of researchers throughout the social sciences. CSISS is funded by the <a href="National Science Foundation">National Science Foundation</a> under its program of support for infrastructure in the social and behavioral sciences.

CSISS News

Upgrade to GeoDa™ 0.9.5-i, DynESDA Replacement

Core Programs	Learning Resources	Spatial Resources	Spatial Tools
CSISS has six research initiatives and a professional	These introductory materials include CSISS Classics and	CSISS has compiled e- journals, bibliographies, and	Spatial Tools Search Engine
development program for	select video clips from the	other spatial resources for	Select Tools
undergraduate instructors.	CSISS summer workshops.	the social sciences.	Links to Portals
Search Engines	CSISS Events	Community Center	GeoDa™
Try out one of our custom	Here's where you'll find	Join the forums, or if your	Tobler's Flow Mapper
search engines to find spatial analysis resources on the Internet.	information and registration for workshops, conferences and specialist meetings.	organization relates to our mission and goals, register as a CSISS affiliate.	personnel, and sitemap. Our Strategic Plan and Annual Reports are also found here.

Core Programs | Learning Resources | Spatial Resources | Spatial Tools | Search Engines | CSISS Events | Community Center | About CSISS | Site Map | Site Search | Contact CSISS | Plug-ins | Privacy Policy | Site Credits | Home

Copyright © 2001-2004 by Regents of University of California, Santa Barbara Webmaster: Gamaiel Zavala

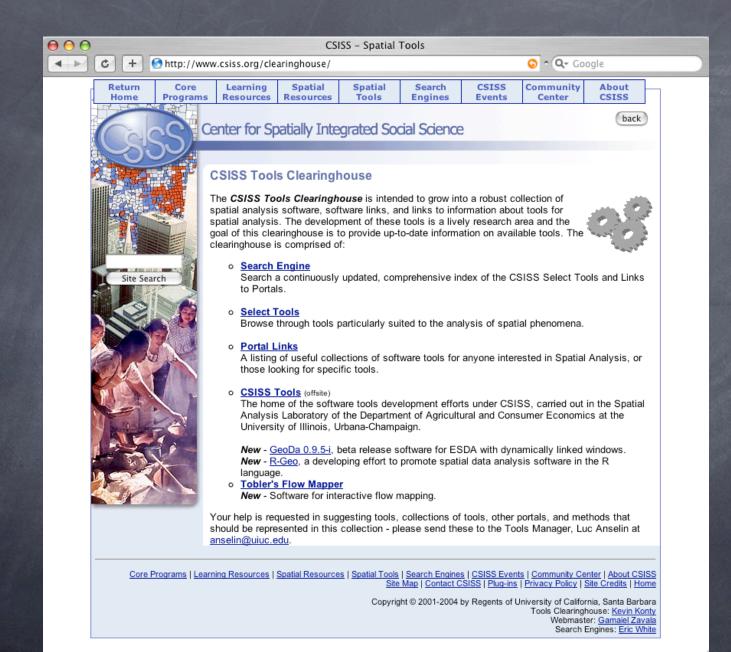
### CSISS Tools Project

#### Goals

- facilitate dissemination of spatial analysis software tools to social scientists
- @ develop a library of spatial data analysis modules
- develop prototypes implementing state of the art methods
- initiate and nurture a community

#### Products

- @ GeoDa
- PySAL and PySpace



## Spatial Analysis and GIS

- Early Efforts (1980s)
  - linking statistical packages and GIS
  - little in terms of spatial statistics
- Linked Spatial Stats and GIS
  - lots of examples in 1990s
    - Arcinfo and SpaceStat, ArcView-DynESDA, ArcView-XGobi, SAGE, using MapObjects, etc.
    - @ geovisualization: cdv, GeoVISTA, ...
  - @ limited functionality, often inflexible architecture
  - slow, limited capacity for larger data sets

## GeoDa Requirements

- Free Standing
  - no GIS
- Modular
  - allow extensibility
- Fast
  - true interactive data exploration, linking and brushing
- Large Data Analysis
  - **100,000**

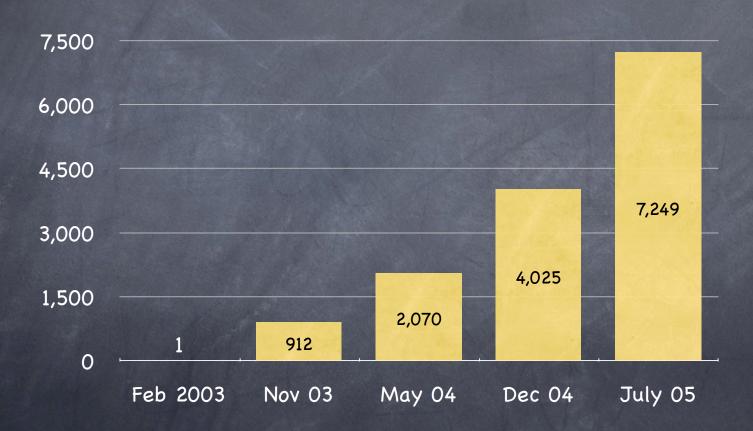
### GeoDa Objectives

- An Introduction to Spatial Data Analysis
  - o visual, interactive, user-friendly
  - path from geo-visualization, EDA and ESDA to spatial regression
  - @ aimed at non (or not yet) GIS users
- Free Download
- Support through OpenSpace Mailing List

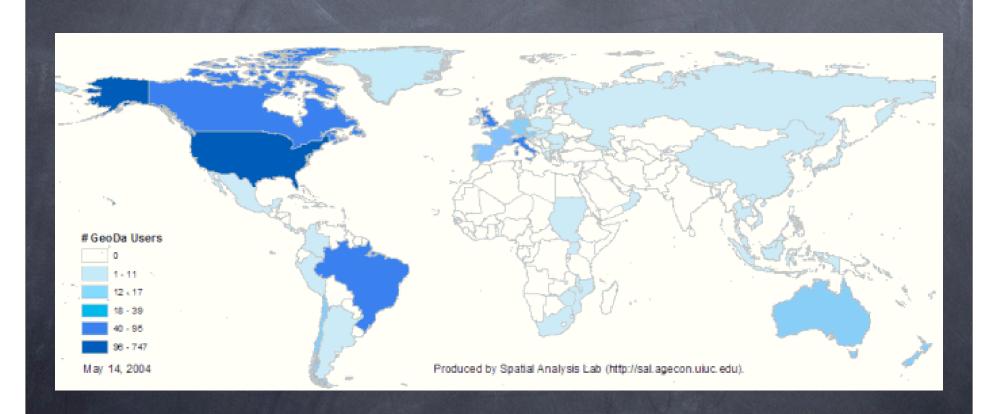
http://sal.uiuc.edu/mailman/listinfo/openspace



#### GeoDa User Base



## Geographical Distribution



# GeoDa & Crime Analysis

#### What GeoDa is designed for

- Analysis of lattice data: Areas & fixed points
  - Events (e.g., address-level crimes) have to be aggregated to areas
  - Estimating underlying risk of crime: Smoothing

#### What GeoDa is <u>not</u> designed for

- Point pattern analysis
  - Event data: Location subject to uncertainty
- Geostatistical analysis
  - Sample points

## Functionality Principles

#### Main Toolbar

1 6

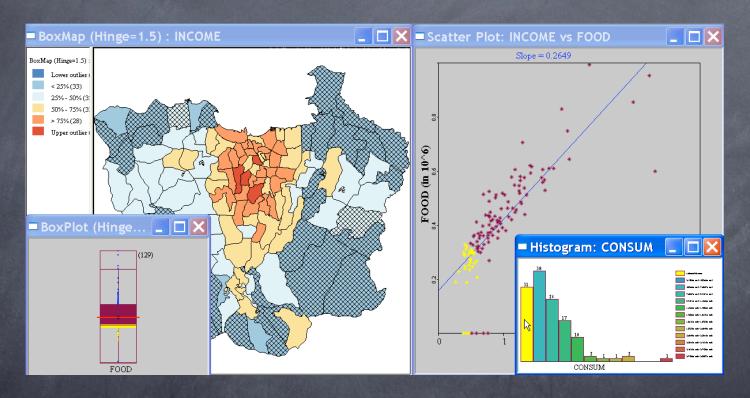


- Data Manipulation (1)
- Mapping (2)
- Spatial Weights (3)
- Multivariate (non-spatial) EDA (4)
- Spatial Autocorrelation (5)
- Spatial Regression (6)

## Linking and Brushing

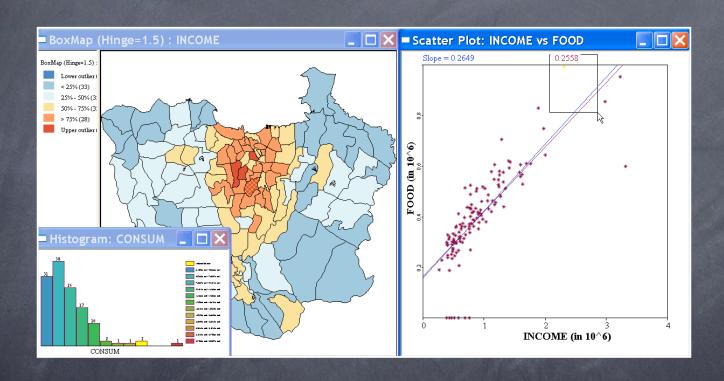
- Dynamic Graphics
  - user interaction with multiple statistical graphs and maps
- Linking
  - selection in one graph is simultaneously selected in all graphs
- Brushing
  - changing the selection is dynamically updated in all graphs and maps

## Linking



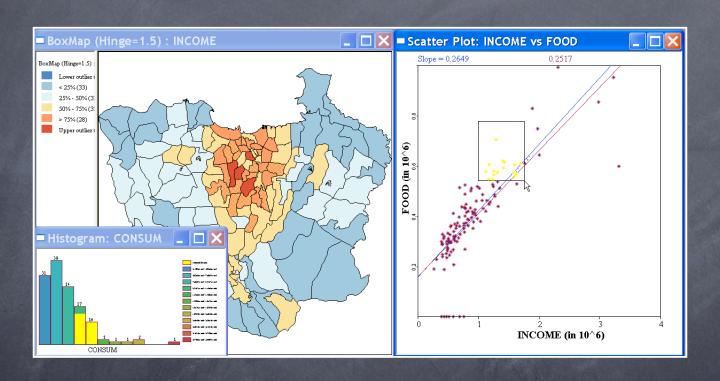
the selected observations in any graph are simultaneously highlighted in all other graphs

## Brushing a Scatter Plot



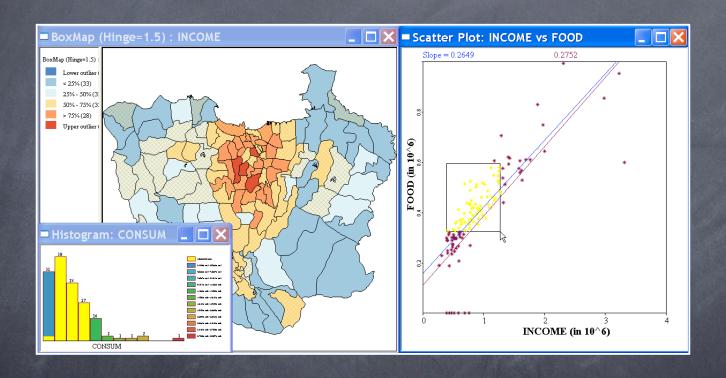
changing the selection in the scatter plot is simultaneously highlighted in all other graphs

## Brushing a Scatter Plot



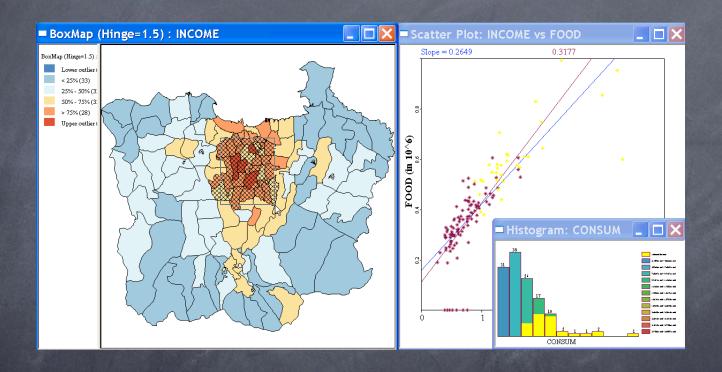
changing the selection in the scatter plot is simultaneously highlighted in all other graphs

## Brushing a Scatter Plot



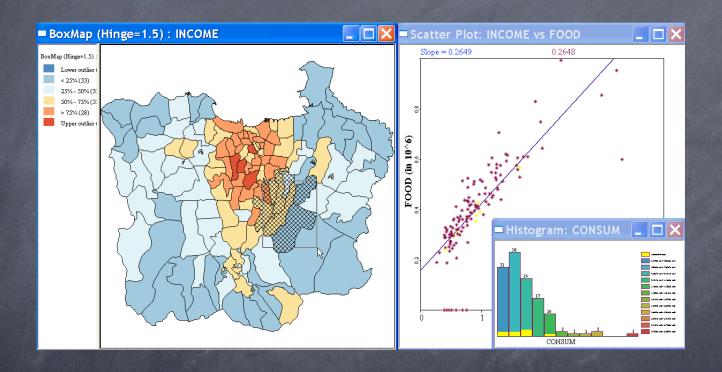
changing the selection in the scatter plot is simultaneously highlighted in all other graphs

## Brushing a Map



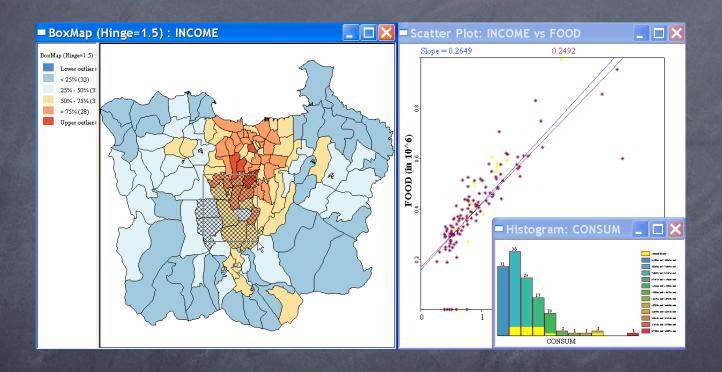
changing the selection in the map is simultaneously highlighted in all other graphs

## Brushing a Map



changing the selection in the map is simultaneously highlighted in all other graphs

## Brushing a Map



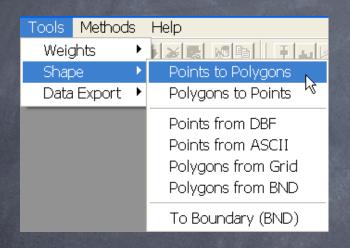
changing the selection in the map is simultaneously highlighted in all other graphs

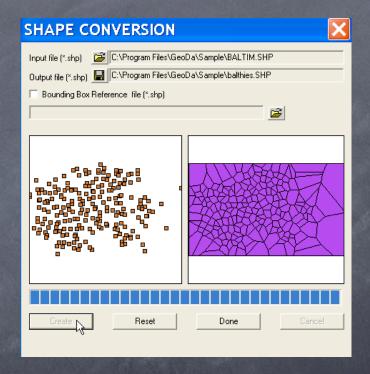
## Functionality Overview

## Data Manipulation

- Input
  - opolygon and point shape files
  - ascii point and boundary files
- Conversion/Creation
  - points to polygons (Thiessen polygons)
  - polygons to points (centroids)
  - regular grids
- Calculation
  - table calculator, rates, smoothing, queries
- Export
  - 6 boundary files, data sets, bit maps

## Thiessen Polygons

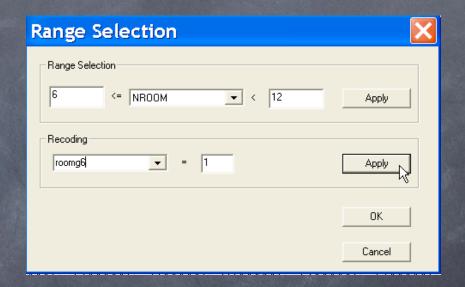




all points in the polygon are closer to the center point than to any other point = market area

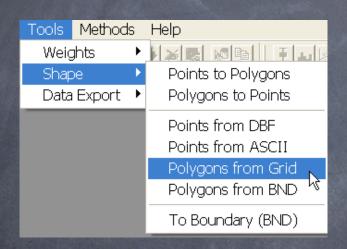
## Create Dummy Variable

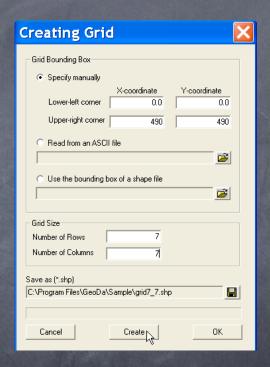




use Table Calculator to create indicator variables that meet specified criteria: both in table and from map (save selected)

## Regular Lattices





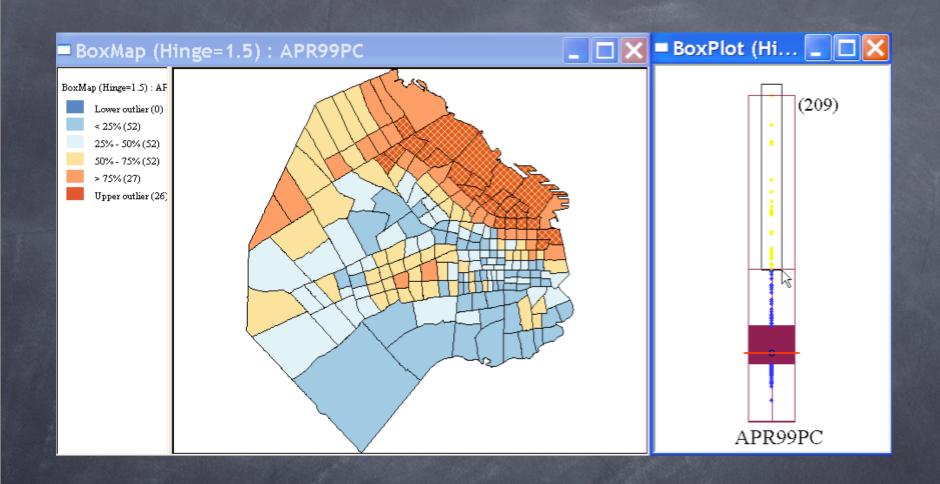
create regular grid by specifying bounding box and number of grid cells

## demonstration

Copyright © 2005 by Luc Anselin, All Rights Reserved

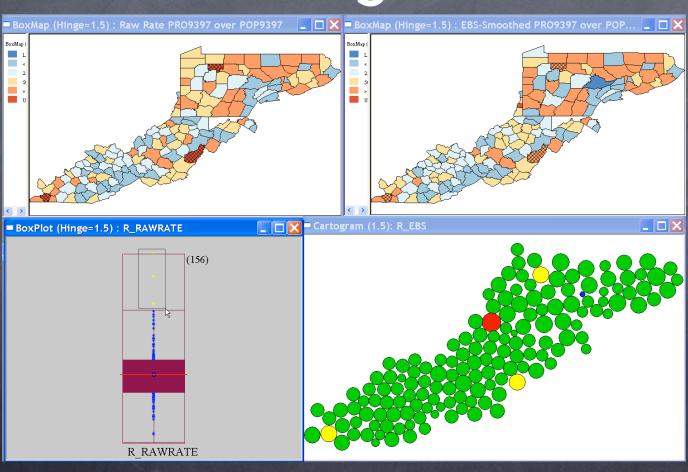
## Mapping

- Choropleth Maps
  - quantile, percentile, standard deviational
- Outlier Maps
  - box map
- Rate Smoothing
  - Empirical Bayes
  - spatial smoothing
- Cartogram
- Map Movie



#### Box Map with Box Plot Buenos Aires Election Results

# Smoothed Rates and Cartogram

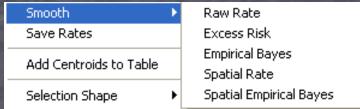


### Rate Smoothing

- Raw rates used to estimate underlying disease risk
- Differences in population size related to problem of variance instability and spurious outliers
- Rate smoothing addresses variance instability by borrowing strength from other spatial units

### GeoDa Smoothing Options

GeoDa contains an excess risk map option and three smoothers:

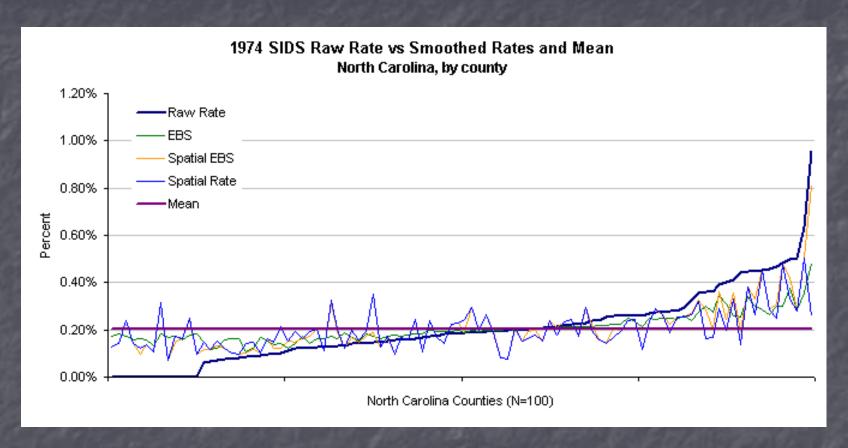


**Excess Risk**: Expected risk based on product of raw rate and average overall risk of all observations

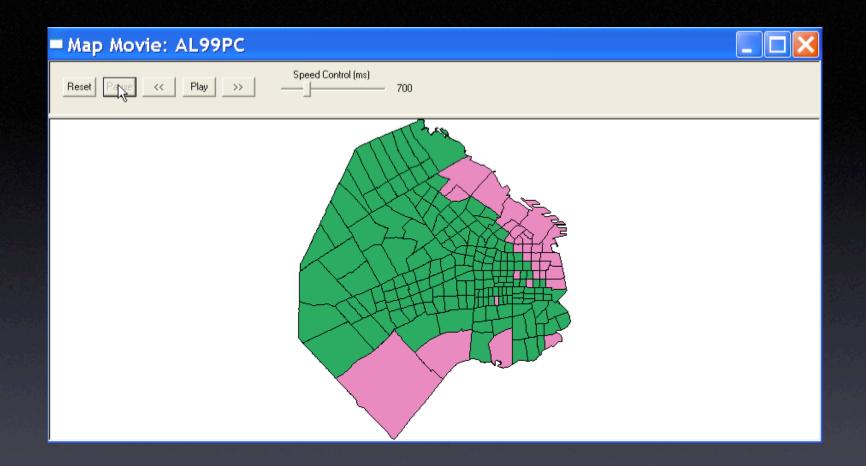
Where Smoothers Borrow Strength From:

- **Empirical Bayes (EBS)**: Overall mean of the underlying risk distribution of all observations
- **Spatial Rate**: Neighbors, as defined in spatial weights matrix
- Spatial Empirical Bayes: Same as EBS but strength not borrowed from all observations, only regional subset

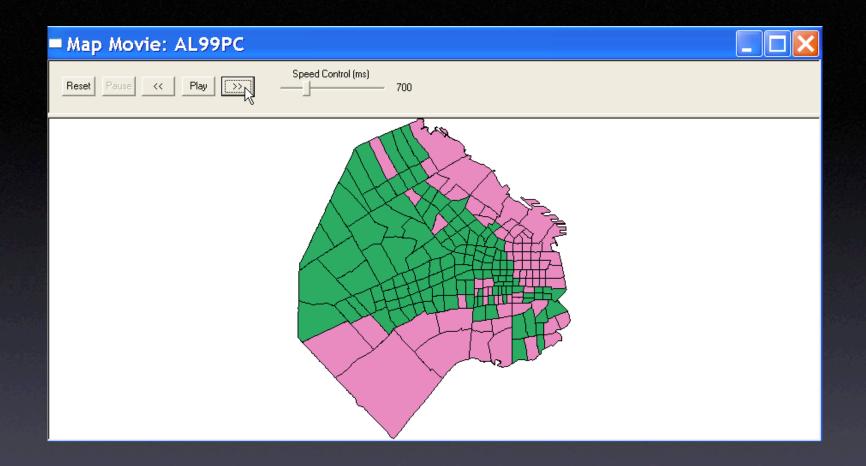
### Rate Smoothing: Comparison



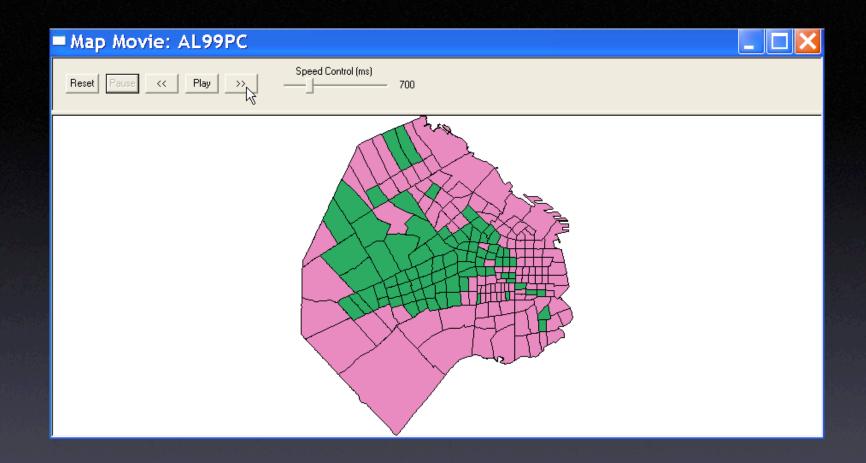
Raw rate compared to smoothed rates and mean



# Map Movie Buenos Aires Election Results



# Map Movie Buenos Aires Election Results



# Map Movie Buenos Aires Election Results

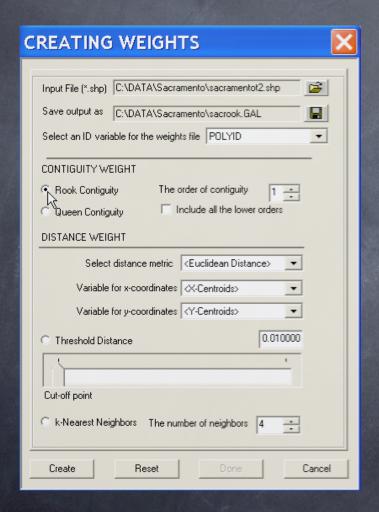
## demonstration

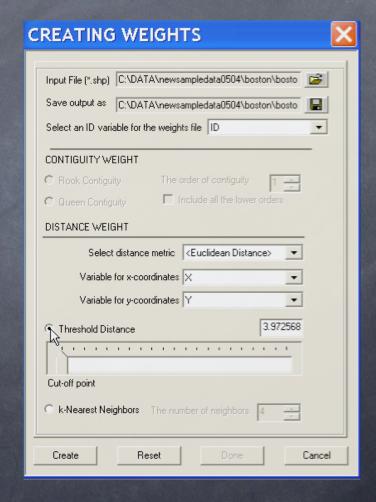
Copyright © 2005 by Luc Anselin, All Rights Reserved

### Spatial Weights

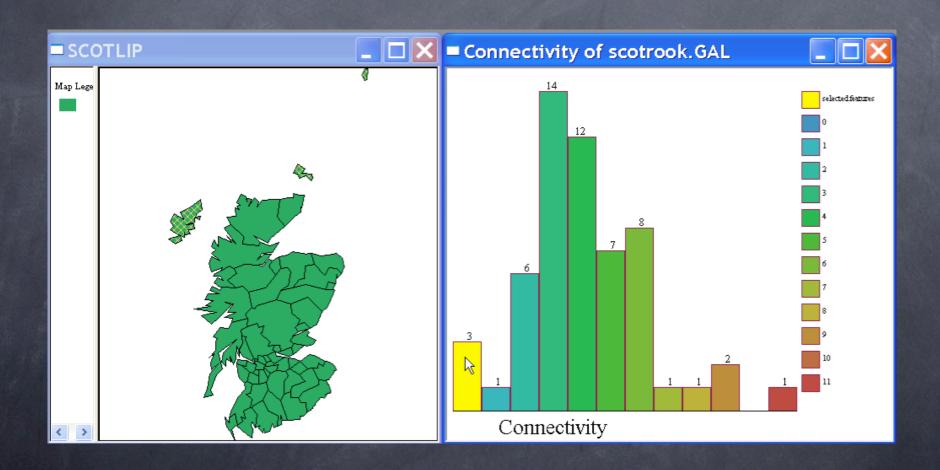
- Contiguity Based
  - orook and queen
  - higher order contiguity
- Distance Based
  - ø distance band, k-nearest neighbors
- Weights Characteristics
  - connectivity, islands

### Weights Dialogs





### Islands

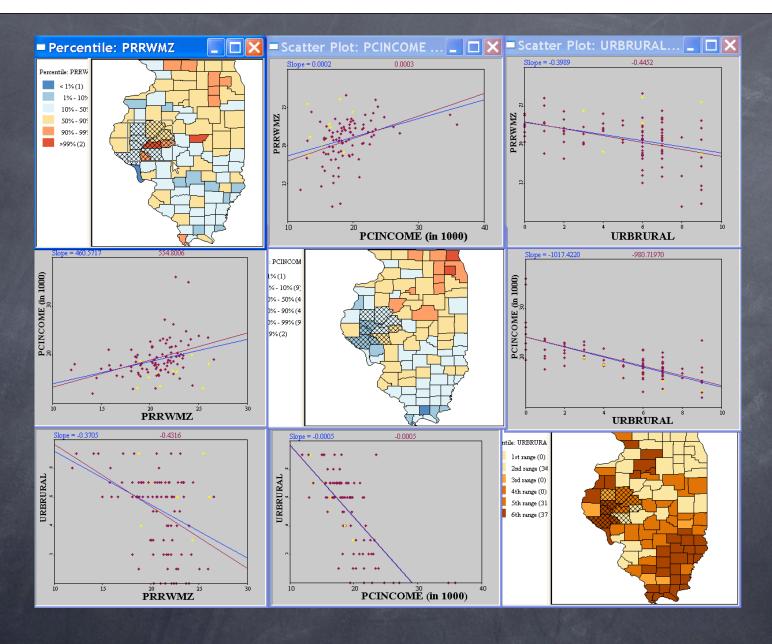


## demonstration

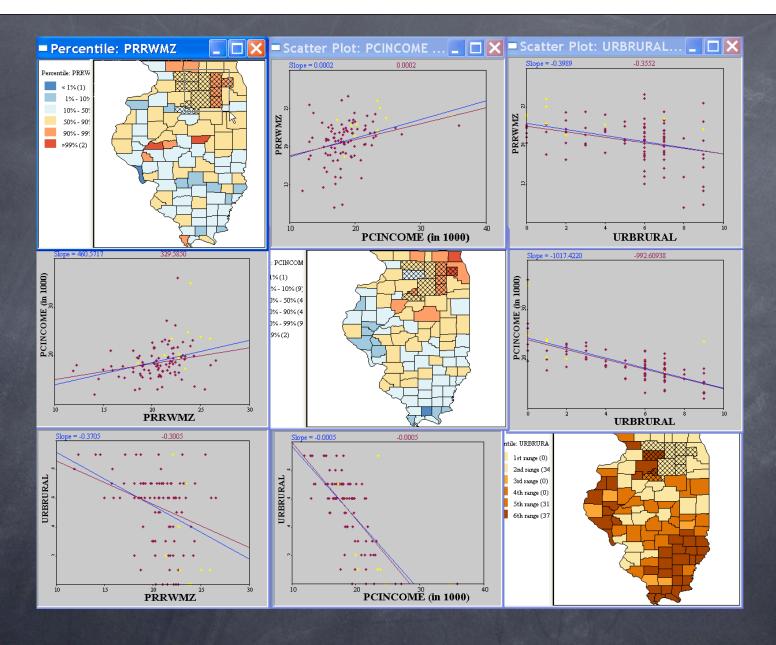
Copyright © 2005 by Luc Anselin, All Rights Reserved

### Multivariate EDA

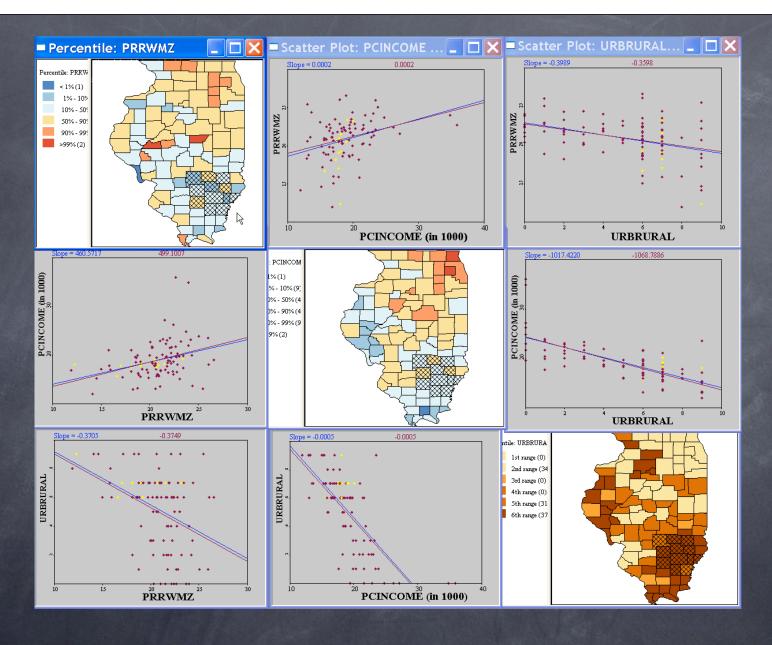
- Scatter Plot Matrix
- Parallel Coordinate Plot (PCP)
- Conditional Plots
  - conditional maps
  - conditional histograms
  - conditional box plots
  - conditional scatter plots
- 3D Scatter Plot



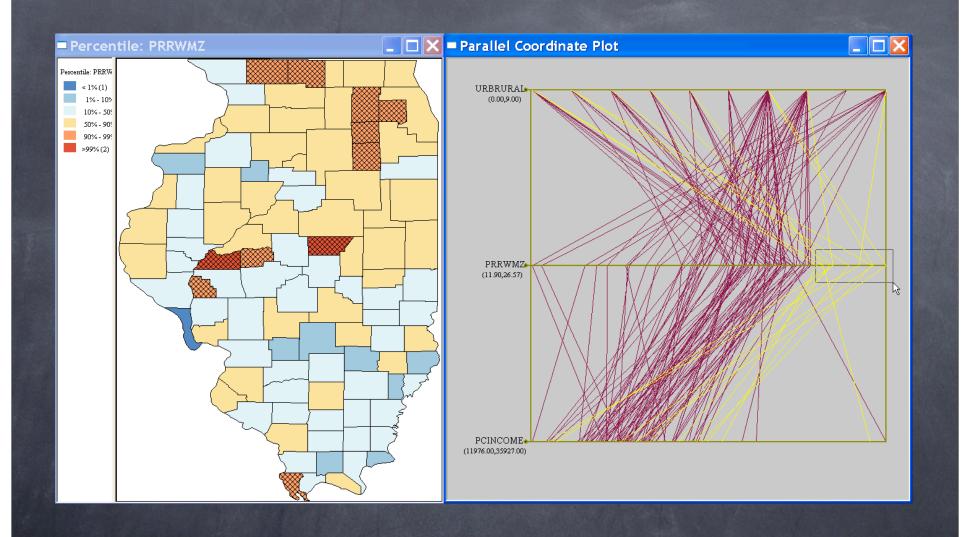
brushing the scatter plot matrix

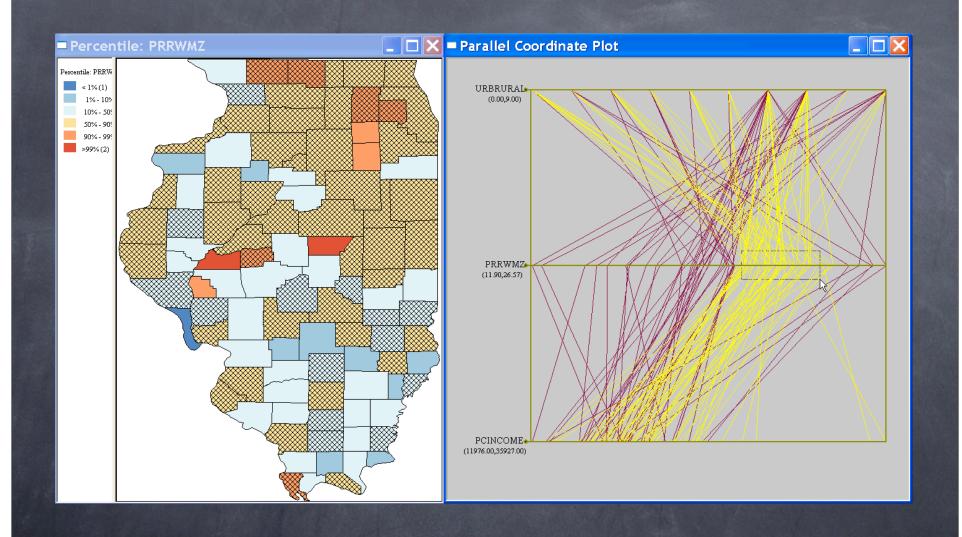


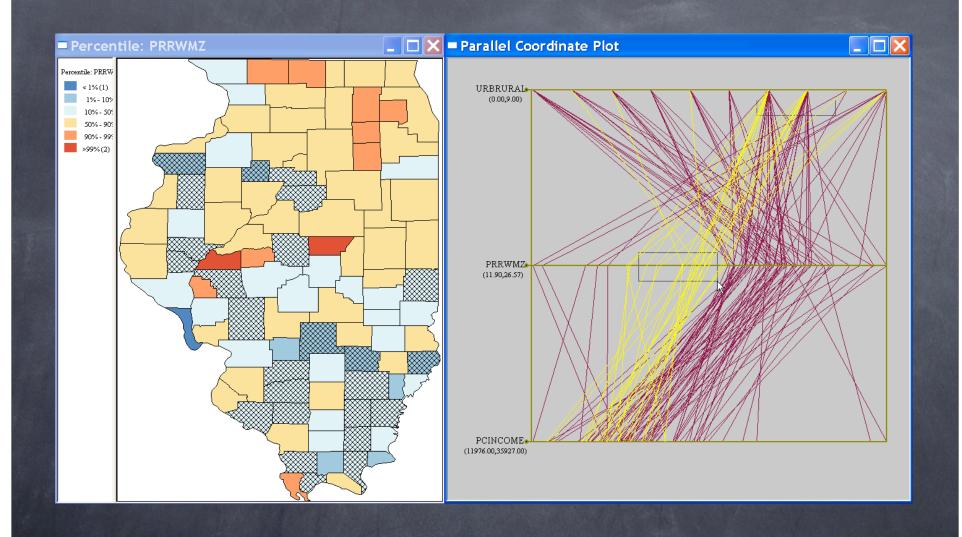
brushing the scatter plot matrix

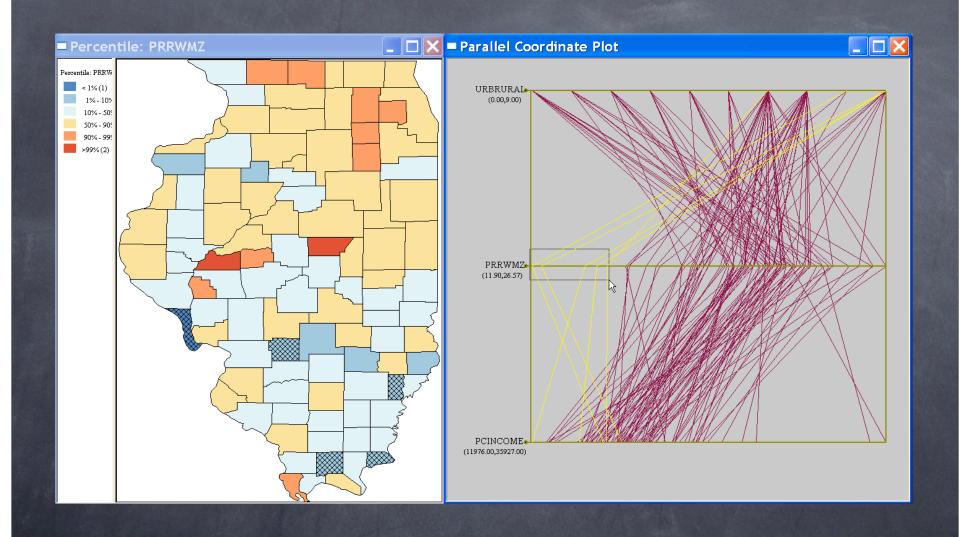


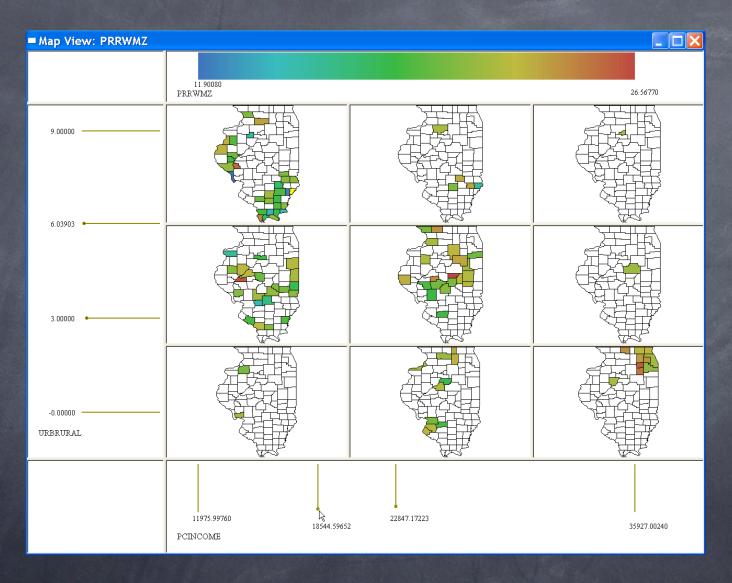
brushing the scatter plot matrix



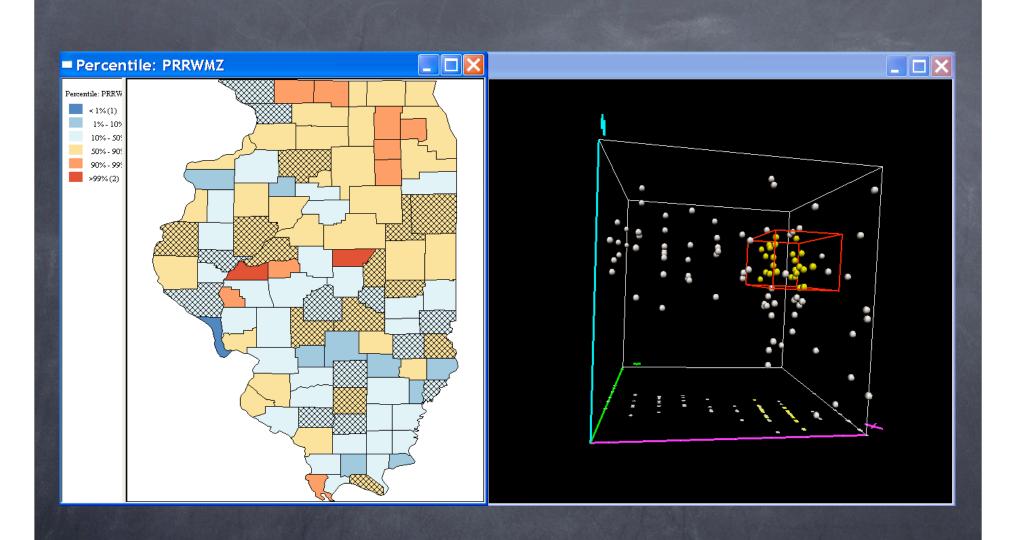








### conditional maps



brushing the 3-D scatter plot

## demonstration

Copyright © 2005 by Luc Anselin, All Rights Reserved

### Spatial Autocorrelation

- Moran Scatter Plot
  - randomization inference
  - © EB adjusted Moran for rates
- Local Moran
  - LISA cluster map and significance map
  - sensitivity analysis
- Bivariate Moran Scatter Plot
- Bivariate Local Moran

### Global and Local Clustering

### Global Moran's I

- What is the extent of clustering in the total area?
- Is this clustering significantly different from a random spatial distribution?

#### Local Moran's I

- Do local clusters (high-high or low-low) or local spatial outliers (high-low or low-high) exist?
- Are these local clusters and spatial outliers statistically significant?

### Global Clustering

Box Map

#### 1990 Homicide Rates

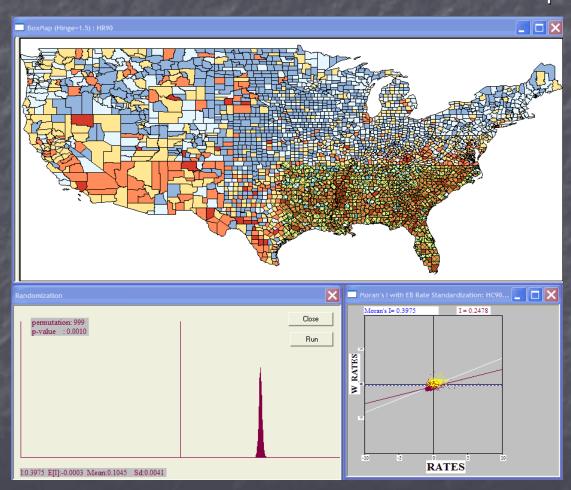
#### Global Moran's I

$$I = \left(\frac{N}{S_0}\right) \frac{\sum_{i} \sum_{j} w_{ij} z_i z_j}{\sum_{i} z_i^2}$$

$$z_i = x_i - \mu$$

$$z_j = x_j - \mu$$

$$S_0 = \sum_{i} \sum_{j} w_{ij}$$



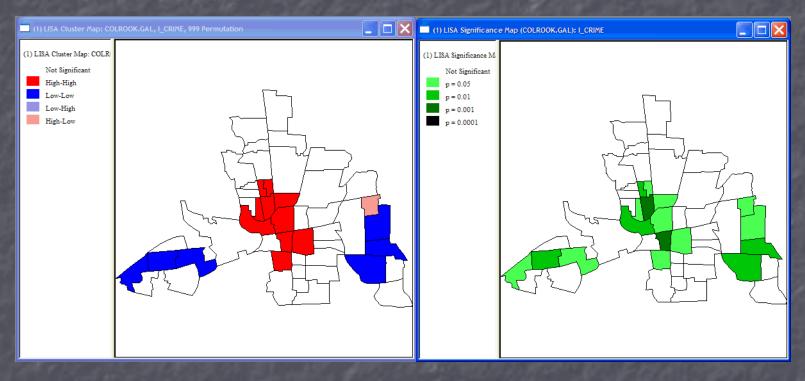
Randomization Test

Moran Scatter Plot

### Local Cluster & Significance Maps

Cluster map

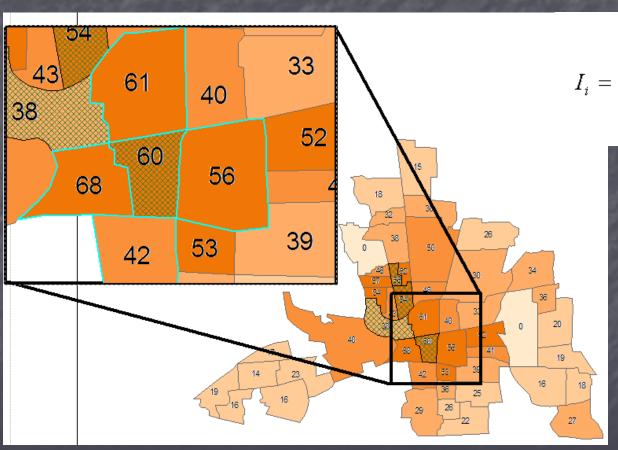
Significance map



Local Indicators of Spatial Association (LISA) maps can be used to identify spatial clusters and outliers at different significance levels

### Computing Local Clusters

Illustration: Mechanics behind computing hi-hi crime cluster



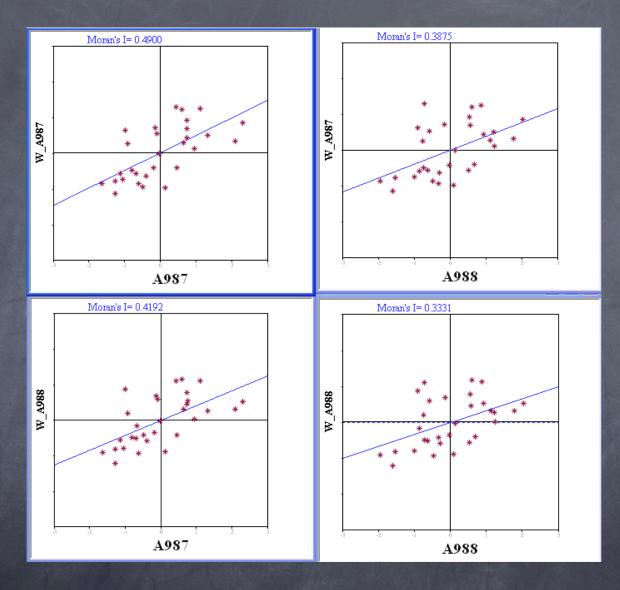
 $I_{i} = \frac{(x_{i} - \mu_{x}) \sum_{j} w_{ij} (x_{j} - \mu_{x})}{\sum_{i} (x_{i} - \mu_{x})^{2} / n}$ 

Cross-product of standardized value for area i and average standardized values of neighbors j, e.g.:

Numerator (mean=57): (60-57)\*[(56-57)+(61-57)+(68-57)+(42-57)]

Denominator: Sum of squared standardized values for each area i in total study area, divided by N

GeoDa uses row-standardized weights (rows sum to one)



Bivariate Moran scatter plot matrix

## demonstration

Copyright © 2005 by Luc Anselin, All Rights Reserved

## Spatial Regression

- OLS with Diagnostics
  - o normality, heteroskedasticity
  - Moran's I
  - Lagrange Multiplier tests
- Maximum Likelihood Spatial Lag
  - asymptotic variance matrix
- Maximum Likelihood Spatial Error
  - asymptotic variance matrix
- Predicted Value and Residual Maps

# OLS with Diagnostics

REGRESSION					
SUMMARY OF OUTP			S ESTIMATION		
Data set : COLUMBUS					
Dependent Varia	ble : C		of Observati		
Mean dependent			of Variables	-	
S.D. dependent	var : 16.	5605 Degree	es of Freedom	: 46	
R-squared	: 0.55	2404 F-stat	istic	: 28.3856 :9.34074e-009	
Adjusted R-squa			?-statistic)	:9.34074e-009	
Sum squared res Sigma-square	idual: 601		kelihood	: -187.377	
S.E. of regress	: 130		e info criterio cz criterion		
Sigma-square MI	10n : 11	435 SCNWai	z criterion	: 386.43	
S.E of regressi	. 122	0794			
a.m of regressi	On ML: II.	0/94			
Variable	Coefficient	Std.Erro	t-Statist	ic Probability	
CONSTANT	68.61896	4.735486	5 14.490	37 0.0000000	
INC	-1.597311	0.3341308			
HOVAL	-0.2739315	0.1031987			
REGRESSION DIAGNOSTICS					
MULTICOLLINEARITY CONDITION NUMBER 6.541828					
TEST ON NORMALI					
TEST	DF	VALUE		_	
Jarque-Bera	2	1.8357	753 0.3	993663	
DIAGNOSTICS FOR HETEROSKEDASTICITY					
RANDOM COEFFICI		ICITI			
TEST	DF	VALUE	PRO:	В	
Breusch-Pagan t		7.9004		192505	
Koenker-Bassett		5.6940		580156	
SPECIFICATION R		J. 0941	0.0	300136	
TEST	DF	VALUE	PRO:	В	
White	5	19.946		012792	
W11200		23.31		010.70	
DIAGNOSTICS FOR SPATIAL DEPENDENCE					
FOR WEIGHT MATRIX : colrook.GAL (row-standardized weights)					
TEST		MI/DF	VALUE	PROB	
Moran's I (erro	r) 0	.249862	2.9376173	0.0033076	
Lagrange Multip	lier (lag)	1	8.7599071	0.0030792	
Robust LM (lag)		1	3.0721737	0.0796429	
Lagrange Multip			5.8148799	0.0158911	
Robust LM (erro	r)	1	0.1271465	0.7214092	
Lagrange Multip		2	8.8870536	0.0117544	
======================================					

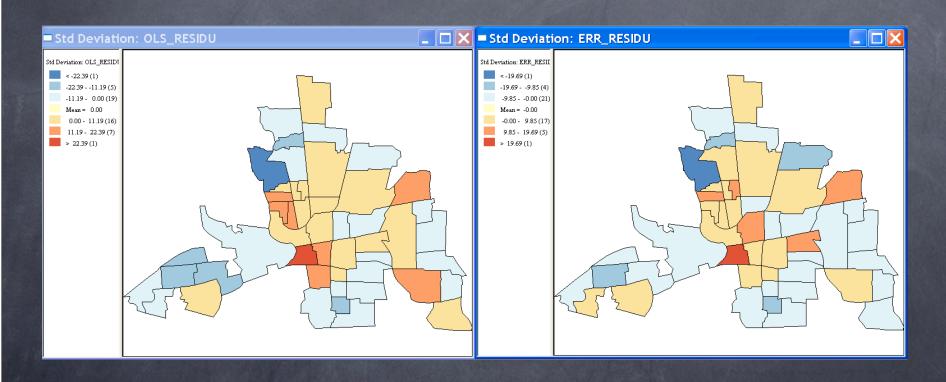
## ML Spatial Lag

#### REGRESSION SUMMARY OF OUTPUT: SPATIAL LAG MODEL - MAXIMUM LIKELIHOOD ESTIMATION Data set : COLUMBUS Spatial Weight : colrook.GAL Dependent Variable : CRIME Number of Observations: 49 Mean dependent var : 35.1288 Number of Variables : 4 S.D. dependent var : 16.5605 Degrees of Freedom : 45 Lag coeff. (Rho) : 0.422808 R-squared : 0.650962 Log likelihood : -182.518 Sq. Correlation : - Akaike info criterion : 373.035 Sigma-square : 95.7235 Schwarz criterion : 380.603 S.E of regression : 9.78384 Coefficient Std.Error z-value Probability W\_CRIME 0.4228079 0.1155777 3.658213 0.0002540 CONSTANT 45.26498 7.175796 6.308008 0.0000000 INC -1.036346 0.3052524 -3.395047 0.0006863 HOVAL -0.2594178 0.08879673 -2.921479 0.0034839 REGRESSION DIAGNOSTICS DIAGNOSTICS FOR HETEROSKEDASTICITY RANDOM COEFFICIENTS $\mathbf{DF}$ VALUE PROB TEST 23.57972 0.0000076 Breusch-Pagan test DIAGNOSTICS FOR SPATIAL DEPENDENCE SPATIAL LAG DEPENDENCE FOR WEIGHT MATRIX : colrook.GAL $\mathbf{DF}$ PROB Likelihood Ratio Test 1 9.719246 0.0018235

## ML Spatial Error

REGRESSION SUMMARY OF OUTPUT: SPATIAL ERROR MODEL - MAXIMUM LIKELIHOOD ESTIMATION						
Data set : COLUMBUS						
Spatial Weight : colrook.GAL						
Dependent Variable : CRIME Num	mber of Observations: 49					
	mber of Variables : 3					
	gree of Freedom : 46					
Lag coeff. (Lambda): 0.548474						
R-squared : 0.653718 R-	squared (BUSE) : -					
Sq. Correlation : - Lo	g likelihood : -181.894632 aike info criterion : 369.789					
Sigma-square : 94.967743 Ak	aike info criterion : 369.789					
Sigma-square : 94.967743 Akaike info criterion : 369.789 S.E of regression : 9.74514 Schwarz criterion : 375.464725						
Variable Coefficient Std.E	rror z-value Probability					
CONSTANT 60.37519 5.32	507 11.33791 0.0000000					
INC -0.9610436 0.3311	456 -2.902179 0.0037059					
HOVAL -0.3031981 0.09264	126 -3.27282 0.0010649					
LAMBDA 0.548474 0.1313						
REGRESSION DIAGNOSTICS DIAGNOSTICS FOR HETEROSKEDASTICITY RANDOM COEFFICIENTS						
TEST	DF VALUE PROB					
Breusch-Pagan test	2 18.10319 0.0001172					
DIAGNOSTICS FOR SPATIAL DEPENDENCE SPATIAL ERROR DEPENDENCE FOR WEIGHT MATRIX : colrook.GAL						
TEST	DF VALUE PROB					
Likelihood Ratio Test	1 10.96521 0.0009284					
======================================						

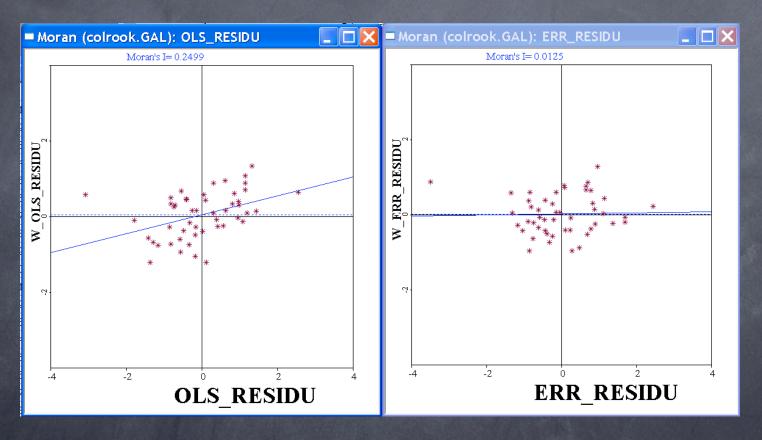
## Residual Maps



OLS residuals

Spatial Error residuals

### Residual Autocorrelation



Moran's I = 0.25

Moran's I = 0.01

# demonstration

Copyright © 2005 by Luc Anselin, All Rights Reserved

# Help System

- Html Based
  - cross-platform
  - hyperlinks
- Resources
  - frequently asked questions (FAQ)
  - troubleshooting and bugs
  - tips
  - index of keywords
  - glossary of terms
  - references

### Help System for GeoDa 0.95i

Welcome to GeoDa's Help system, which you can access by searching the entire system or by selecting links under Resources or the How-To topics below. GeoDa's two <u>user's guides</u> contain additional information. A search function of the system is under development.

If your question is not addressed, please post it on the <u>Openspace mailing list.</u> If you have suggestions for improving GeoDa's help system, please send us an <u>email</u>.

Most of the links in the help system are internal. However, several links access resources on the internet (such as links to *Openspace* threads). If you are using the help system without an internet connection, you will receive "Page not Found" error messages in these instances.

#### Resources

- Frequently Asked Questions (FAQ)
- Troubleshooting and Bugs
- Tips
- Index of Keywords
- Glossary of Terms
- References (including to GeoDa's Algorithms)

#### How to Use GeoDa's Features

#### Getting Started: Input, Mapping and Table Operations

- · Getting Started with GeoDa
  - Load shape file menu options -
- Creating Choropleth Maps
  - Quantile Percentile Box Std Dev Maps Selection -
- Basic Table Operations
  - Select sort query new fields -
- Creating a Point Shape File
  - Input formats import as point shape file -
- o Creating Polygon Shape Files
  - Polygon from boundary file and grid join data -
- Transforming Point and Polygon Shape Files
  - Polygons to central points and text add centroids points to Thiessen polygons -

### **Creating Choropleth Maps**

- Make a simple choropleth map
- Select items in the map
- · Change the selection tool and color

### Make a simple choropleth map

- After a <u>shape file</u> is loaded, you can adjust the width of the legend by dragging the separator between the two panes.
- 2. To choose a map type, right-click on the map and go to Choropleth Map.
- 3. There are four map options:
  - Quantile Map (or m)
  - Percentile Map (or
  - Box Map with hinge 1.5 (or i) and Box Map with hinge 3 (or i)
  - Standard Deviation Map (or [6]).
- Select a variable.
- Optionally, specify the selected variable as the default for future operations (undo the default selection at Edit>Select Variables).
- 6. For the quantile map, specify the number of categories (maximum 9).
- 7. To create another map based on the same shape file, click on ...
- 8. To zoom in, zoom out, or go back to the full extent of the map, right-click and go to Zoom.
- 9. To change the color of the map, right-click and go to Color>Map.
- 10. To return to the default version of the map as it appeared at start-up, go to Map>Reset.
- 11. To export the map, go to Edit>Copy to Clipboard or go to File>Export>Capture to File (the legend needs to be copied/saved separately) or take a <u>screenshot</u> of the map.

#### **Troublehooting & Tips**

- 1. Problems with quantile map categories.
- 2. Taking a screenshot of your GeoDa output.

### Index

This page contains an index of the key words and terms used in GeoDa, listed in alphabetical order.

Most of the links in the help system are internal. However, several links access resources on the internet (such as links to *Openspace* threads). If you are using the help system without an internet connection, you will receive "Page not Found" error messages in these instances.

#### A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

#### Α

Add Layer How To Tips

Autocorrelation spatial autocorrelation



#### В

Base Variables

event and base variables

Box Map

How To

**Box Plot** 

How To

References

**Brushing** 

How To

References



### **Glossary of Terms**

This page contains definitions of the key terms referred to in the help system, listed in alphabetical order. Where applicable, it also provides links to:

- o how-to pages ("HowTo" icon),
- o troubleshooting ("Trouble" icon),
- tips
- o references ("Books" icon), and
- o references containing the formulas implemented in GeoDa ("Formula" icon).

Most of the links in the help system are internal. However, several links access resources on the internet. If you are using the help system without an internet connection, you will receive "Page not Found" error messages in these instances.

#### A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

Α

#### Autocorrelation

See Spatial Autocorrelation.



В

#### **Base Variables**

See Event and Base Variables.

#### **Box Map**

Since box maps are based on the same methodology as box plots, they can be used to detect outliers in a stricter sense than is possible with percentile maps. Box maps group values such as counts or rates into six fixed categories: Four quartiles (1-25%, 25-50%, 50-75%, and 75-100%) plus two outlier categories at the low and high end of the distribution.

Values are classified as outliers if they are 1. 5 times higher than the interquartile range (IQR). IQR is the difference between the 75th percentile (Q3) and the 25th percentile (Q1) or Q3-Q1. It describes the range of the middle of the distribution since 25% of values are above the interquartile range and 25% below it.



# demonstration

Copyright © 2005 by Luc Anselin, All Rights Reserved

# What Next Cross-Platform OpenGeoDa

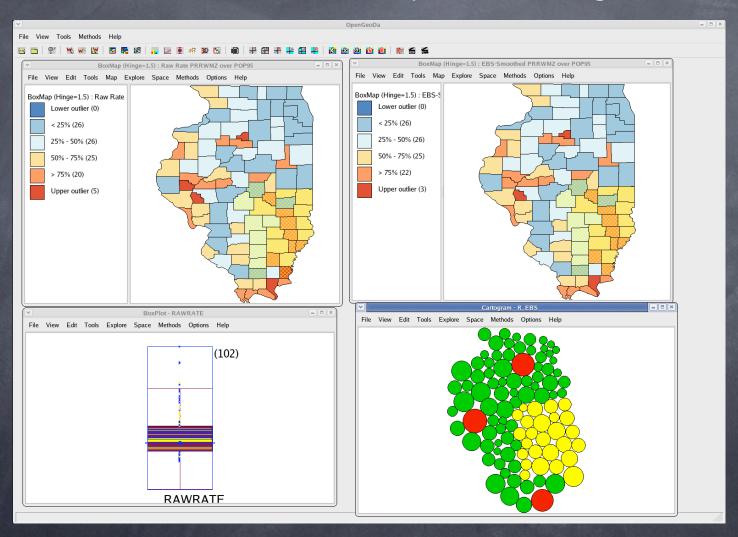
## Motivation

- Growing demand for open source tools
  - 6 third world
  - @ education, non-profit
  - open standards
- Beyond Windows limitations
  - remove constraints embedded in MS Windows
  - allow port to supercomputing (unix/linux) etc.
  - exploit MacOSX graphics
- Run GeoDa on my Mac

# Approach

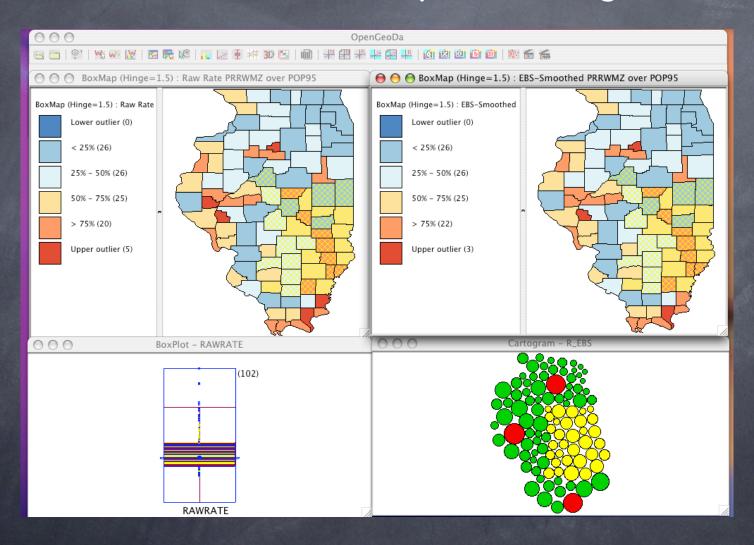
- Remove MFC
  - use cross-platform GUI classes, wxWidgets
- Replace MapObjects
  - recreate mapping functionality without MapObjects
  - use OpenGL and other open source graphics libraries
- Make C++ code cross-platform
  - remove dependencies on MS VC++
  - create make files to handle platform-specific issues
- Not as simple as it sounds ...

## Rates, Outlier Maps, Cartogram



Linux

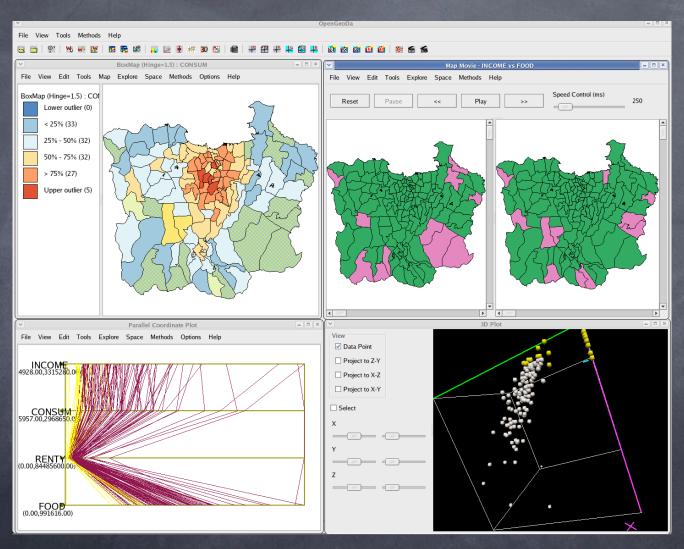
## Rates, Outlier Maps, Cartogram



MacOS X

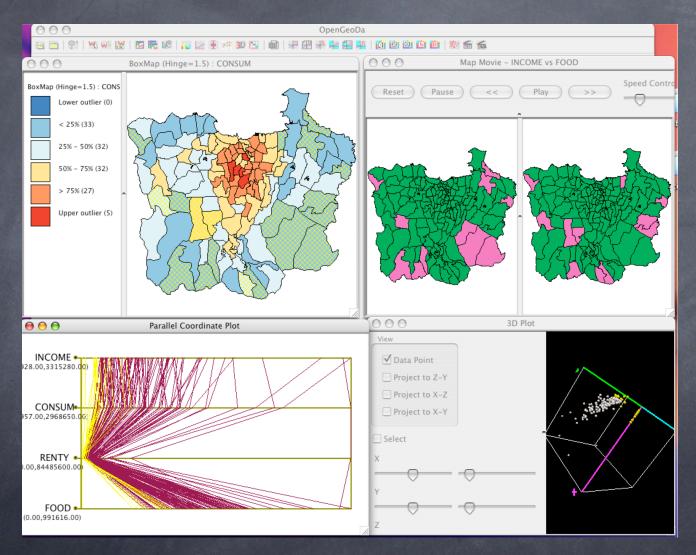
Copyright © 2005 by Luc Anselin, All Rights Reserved

### Multivariate ESDA



### Linux

### Multivariate ESDA



MacOS X

## The Future

- GeoDa is here to stay
  - growing user base
- Completing cross-platform port
  - open source project
- Adding new functionality
  - generalized spatial weights
  - bivariate maps
  - IV and GM estimation
  - (enter favorite technique here) ...

## Resources

- http://geoda.uiuc.edu
- Anselin (2005) Exploring Spatial Data with GeoDa: A Workbook (226pp)
- Anselin, Syabri, Kho (2005) GeoDa, an introduction to spatial data analysis. Geographical Analysis (forthcoming)